

# Bandwidth Allocation with Processing Constraints

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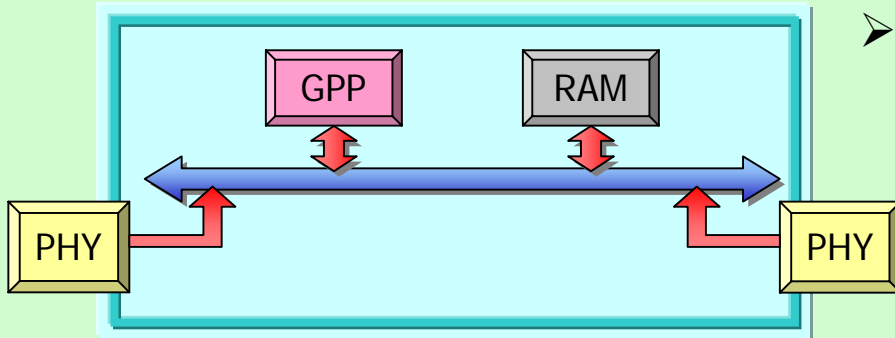
# Outline

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- Introduction
- Resource Allocation Principle
- System Model
- Flow Control Algorithm
- Equilibrium, Fairness & Stability
- IXP1200 Implementation & Performance Results
- Conclusion
- References

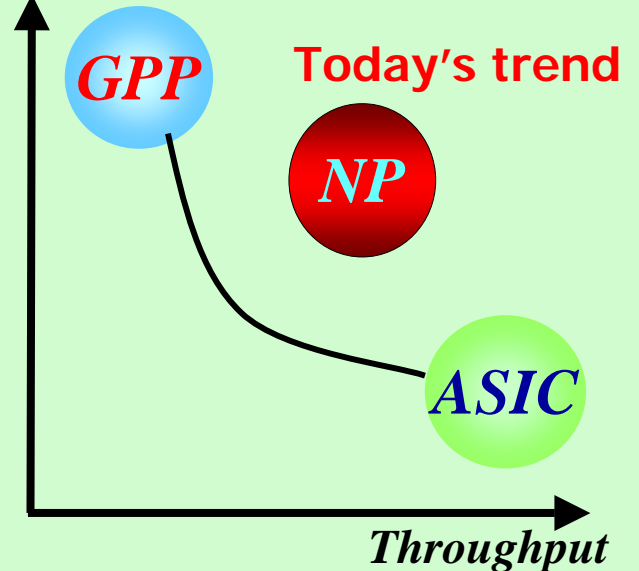
# Introduction

- The evolution of router architecture
  - ❖ GPP-based architecture

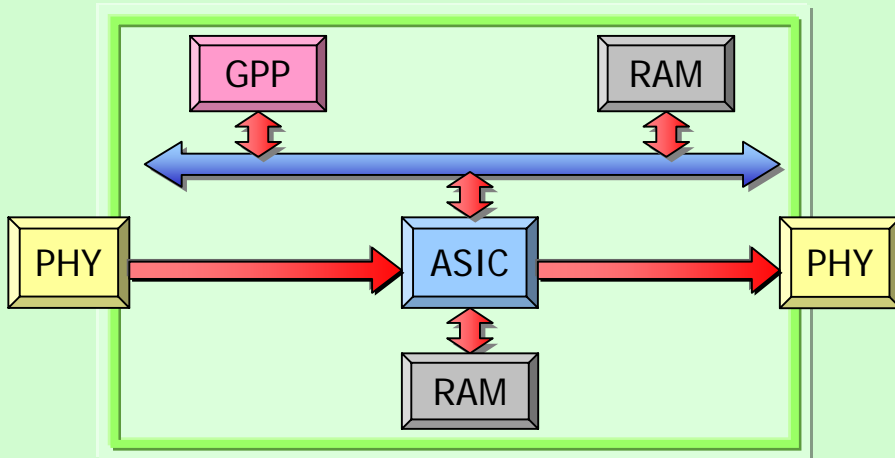


- All packets are processed by GPP.

*Flexibility*



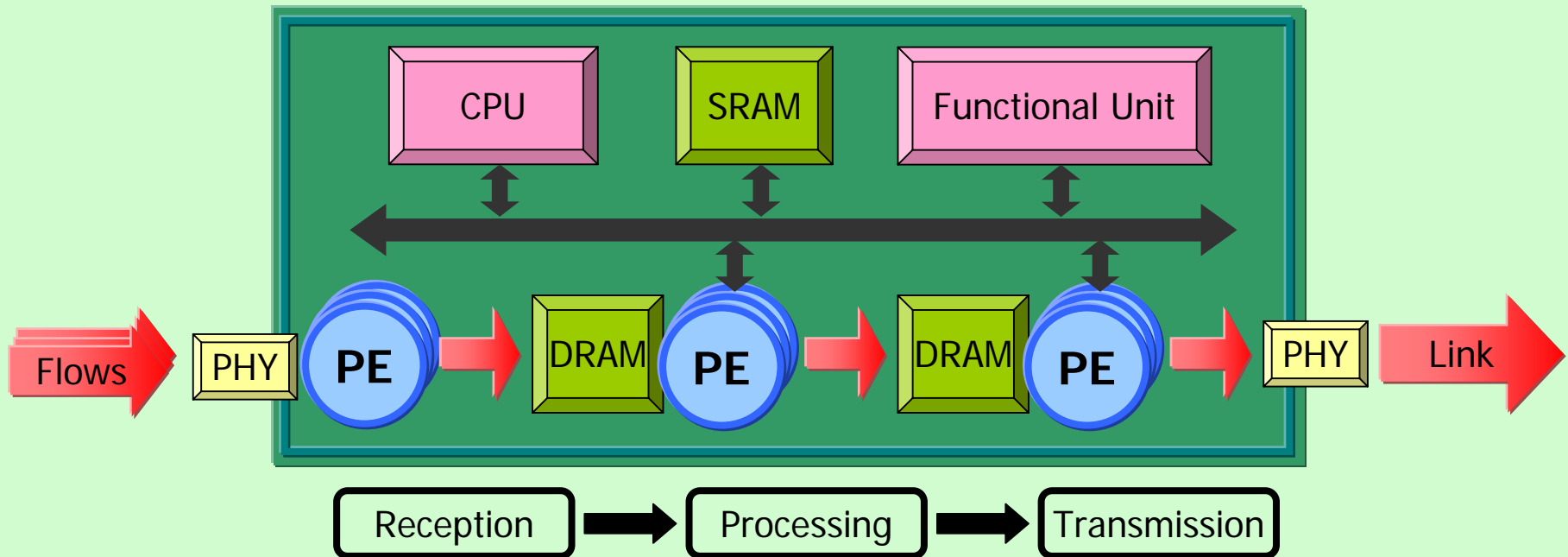
- ❖ ASIC-based architecture



- ASIC processes the majority of packets and GPP processes unusual packets.

# Introduction

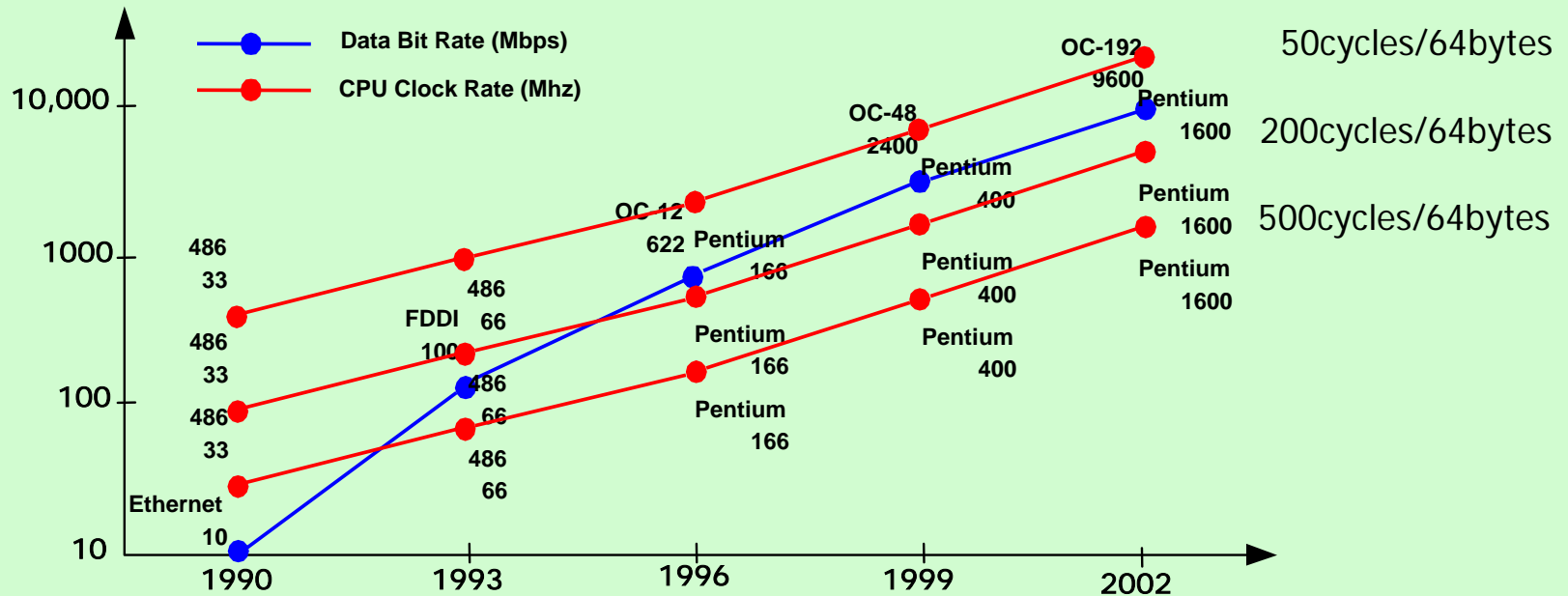
- Logical architecture of a general NP-based node [Johnson 2002]



- ❖ A network processor is mainly used for packet processing which includes CRC check, routing table look-up, header modification, and other extra processes for various network services and algorithms.

# Introduction

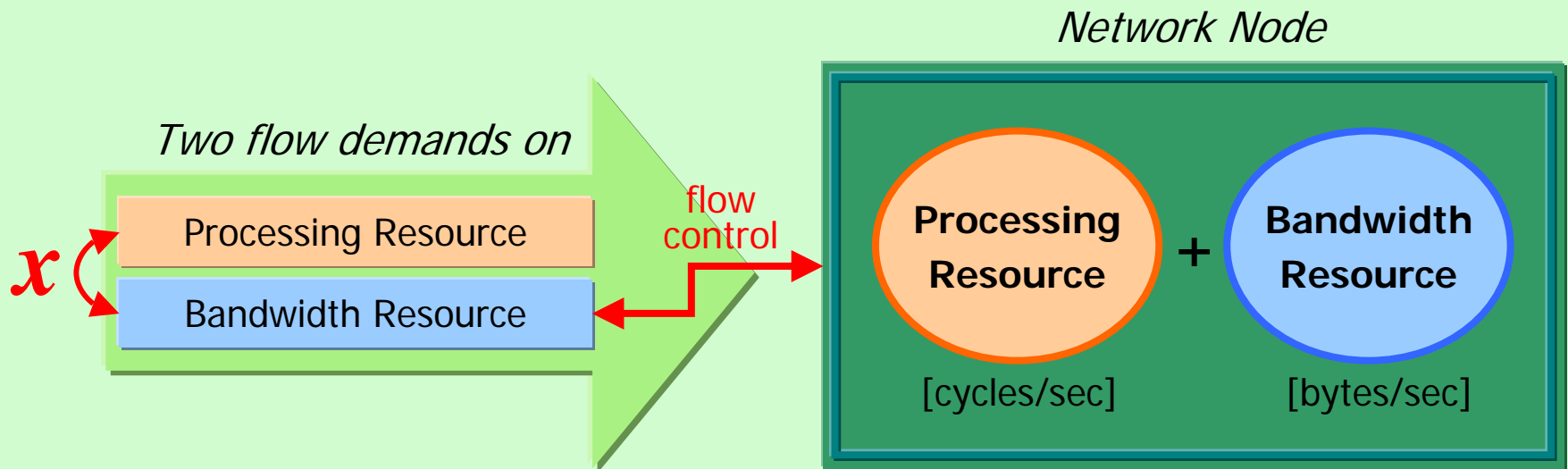
- Network BW & silicon speed growth [Herity 2001]
  - ❖ CPU speed : X 2.7 / 3year (by Moore's Law)
  - ❖ Link capacity : X 4 / 3year



**Hard to predict which resource to be bottlenecked !!**

# Introduction

- ❑ Two-dimensional paradigm in flow control
  - ❖ Should consider both processing resource and bandwidth resource.
  - ❖ Hard to know the flow demand on processing resource until the processing completes.
  - ❖ Can control flows only in terms of “bytes/sec”.



# Packet Processing

- ❑ CommBench [9]: A telecommunications benchmark for network processors
- ❑ Header processing applications (HPA)
  - ❖ RTR: lookup on tree data structures
  - ❖ FRAG: header modifications and checksum
  - ❖ DRR: packet scheduling
  - ❖ TCP: pattern matching on header fields
- ❑ Payload processing applications (PPA)
  - ❖ CAST: encryption/decryption
  - ❖ ZIP: data compression
  - ❖ REED: forward error correction (FEC)
  - ❖ JPEG: media transcoding (DCT, Huffmann coding)

HPA	64	576	1536
TCP	10.3	1.2	.4
FRAG	7.7	.9	.3
DRR	4.1	.5	.2
TCP	2.1	.2	.1

(bytes)

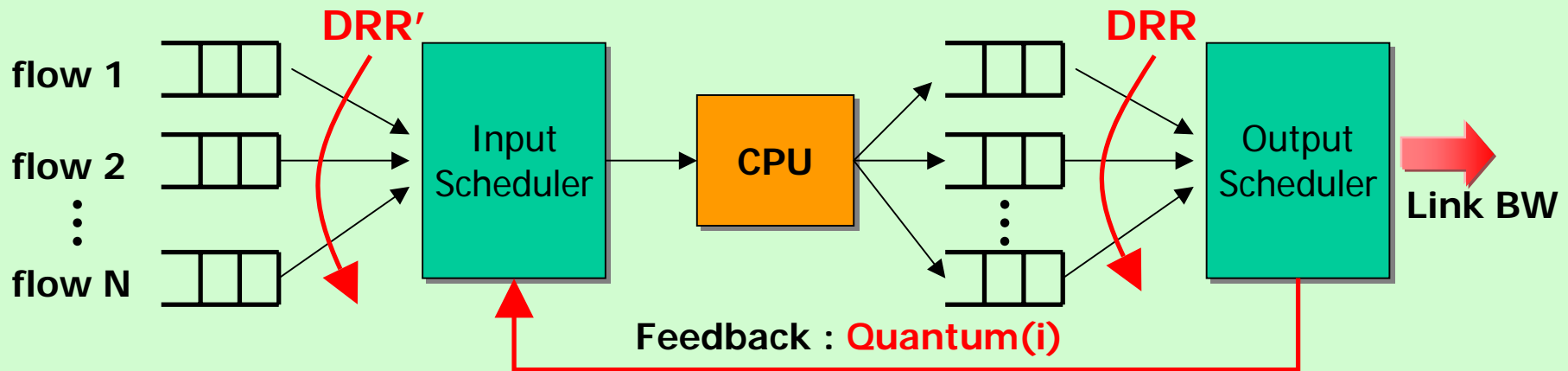
(instructions per byte)

PPA	enc	dec	
REED	603	1052	
ZIP	226	35	
CAST	104	104	
JPEG	81	60	

(instructions per byte)

# Previous Work

- ❑ “Fair Resource Allocation in Active Networks” [Ramachandra 2000]



## ❖ Fairness:

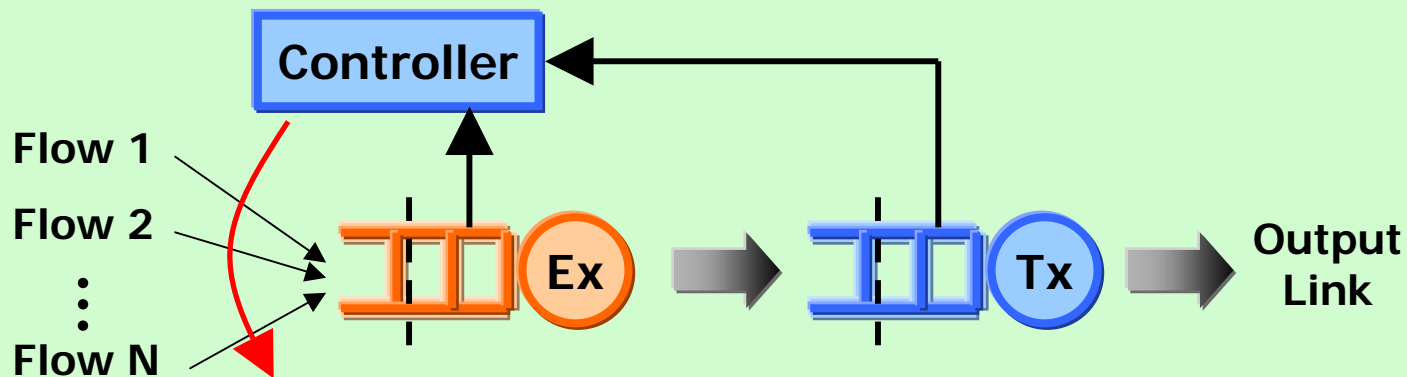
- “CPU\_allocation(i) + BW\_allocation(i)” is to be equalized.

## ❖ Weakness:

- Two-stage DRR scheduling → Complex
- Per-flow queueing → Not scalable
- No buffer control → Internal loss



# Our Approach



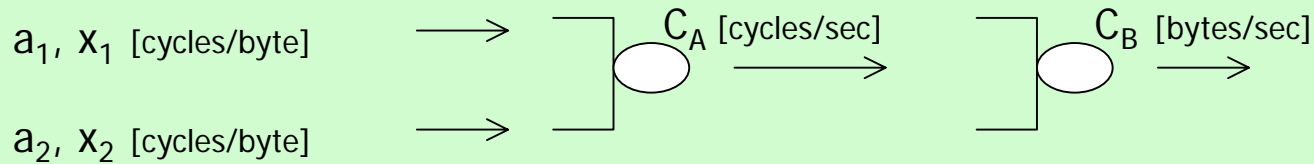
## ❑ Fairness

- ❖ If  $BW > CPU$ , allocate CPU MAX-MIN fair rate.
- ❖ If  $BW < CPU$ , allocate BW MAX-MIN fair rate.
- ❖ Otherwise, allocate the weighted average of above two rates.

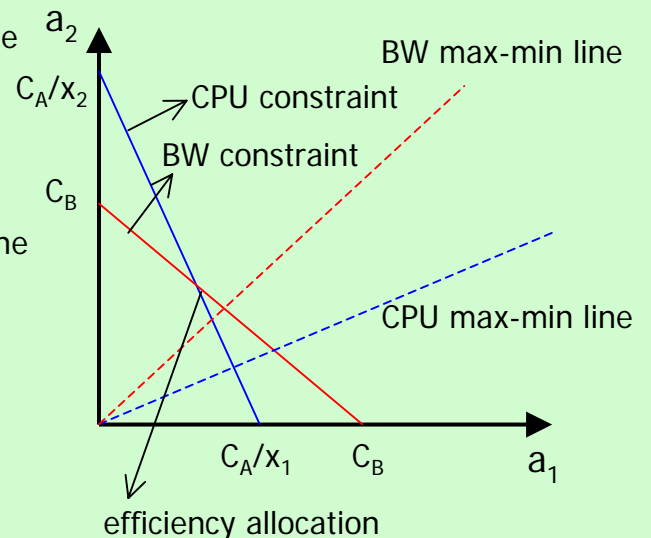
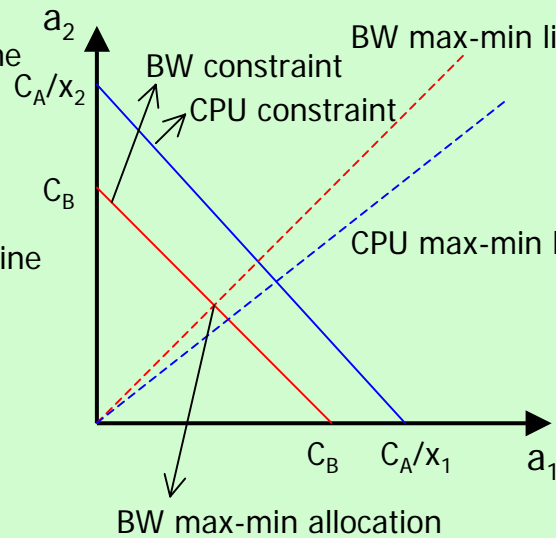
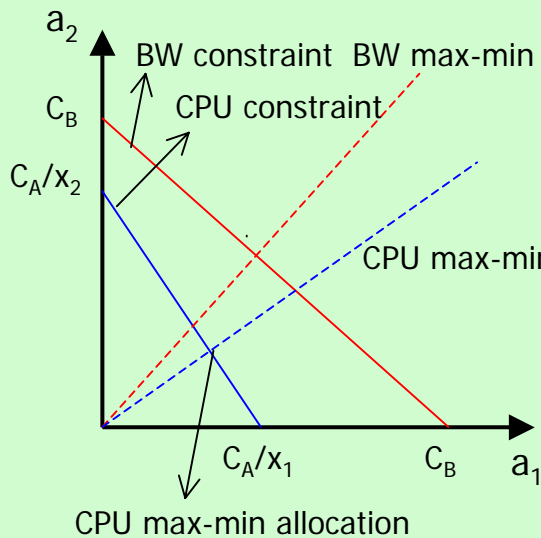
## ❑ Control

- ❖ FIFO queueing → **Simple**
- ❖ No per-flow queueing → **Scalable**
- ❖ Joined control of rate & queue length → **No internal loss**

# Resource Allocation Principle

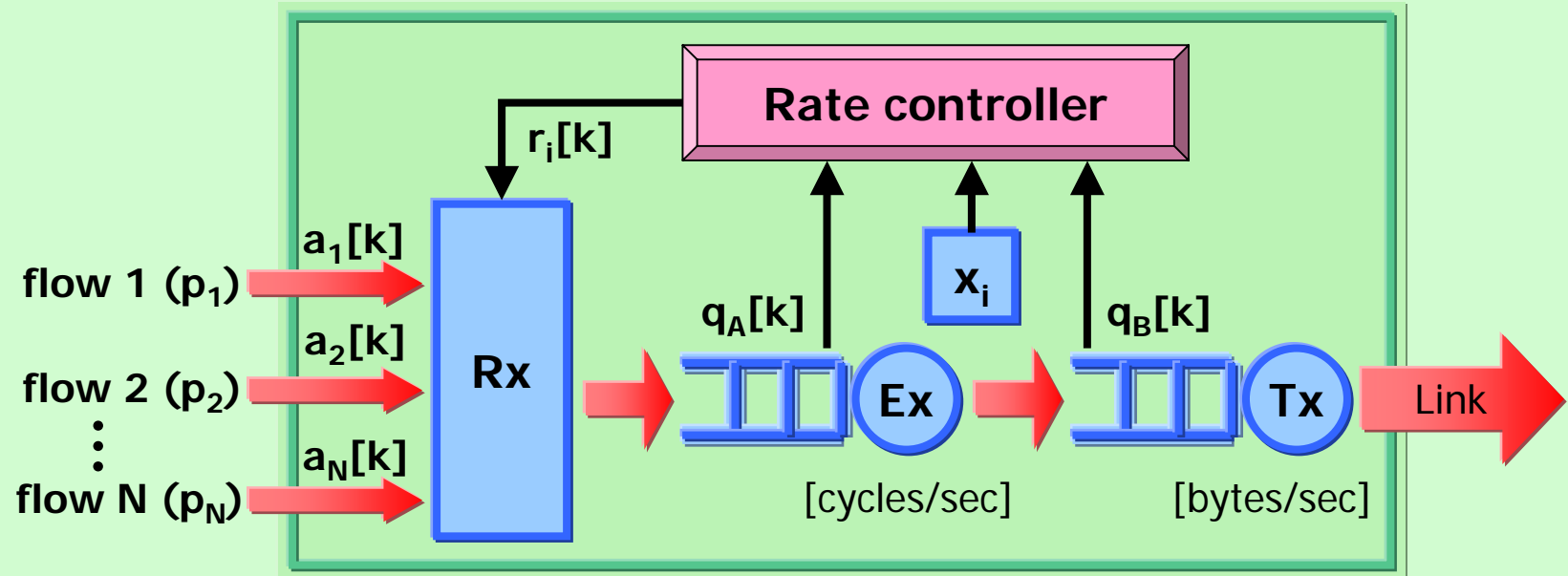


$$\begin{cases} a_1 x_1 + a_2 x_2 \leq C_A & : \text{CPU constraint} \\ a_1 + a_2 \leq C_B & : \text{BW constraint} \end{cases}$$



# System Model

- System model of a NP-based node employing the proposed approach



❖ Injected flow rate :  $a_i[k] = \min(p_i, r_i[k])$

❖ Processing density :  $x_i = \frac{\text{demand for processing resource}}{\text{demand for bandwidth resource}}$  [cycles/byte]  
(the only per-flow state)

# Flow Control Algorithm

- Processing density update : EWMA Filter

$$\text{for every packet, } x_i = (1 - \alpha)x_i + \alpha \left( \frac{\text{processing time}}{\text{packet length}} \right) \quad (0 < \alpha < 1)$$

- Fair rate (FR) is computed in two steps

- ❖ Intermediate FR computation is based on PI control (**BW MAX-MIN**)

$$r[k] = \left[ r[k-1] - \frac{A}{|Q|} (q[k-1] - q[k-2]) - \frac{BT}{|Q|} (q[k-1] - q_T) \right]^+$$

$q[k]$  : total queue length (  $q_A[k] + q_B[b]$  )

$q_T$  : target length of total queue

$A, B$  : control gain

$T$  : control period

$Q$  : set of bottlenecked input flows (  $|Q|$  is the cardinality of  $Q$  )

# Flow Control Algorithm

- ❖ Final FR computation (**CPU MAX-MIN & BW MAX-MIN**)

$$r_i[k] = \left( \frac{q_T - q_B[k-1]}{q_T} \right) \frac{\frac{1}{x_i}}{\sum_{i \in Q} \frac{1}{x_i}} |Q| r[k] + \left( \frac{q_B[k-1]}{q_T} \right) r[k], \quad \forall i \in N$$

## □ Intelligent behavior of the algorithm

- ❖ When processing resource is the bottleneck, allocate CPU MAX-MIN rate.
- ❖ When bandwidth resource is the bottleneck, allocate BW MAX-MIN rate.
- ❖ When both resources are bottlenecked together, determine the degree of bottleneck intensity of each resource and allocate rate as a convex combination of CPU MAX-MIN rate and BW MAX-MIN rate.

# Steady State Solutions

- Three steady state solutions according to  $C_A$ ,  $C_B$ , and the following two averages of  $x_i$ .

$$\bar{x}_n = \frac{\sum_{i \in Q} x_i}{|Q|} \quad (\text{numerical avg.}), \quad \bar{x}_h = \left( \frac{\sum_{i \in Q} \frac{1}{x_i}}{|Q|} \right)^{-1} \quad (\text{harmonic avg.})$$

- ❖ If  $C_A^* \geq \bar{x}_n C_B^*$  (bandwidth resource is the bottleneck),

$$q_A^* = 0, \quad q_B^* = q_T, \quad a_i^* = \frac{C_B}{N}$$

- ❖ If  $C_A^* \leq \bar{x}_h C_B^*$  (processing resource is the bottleneck),

$$q_A^* = q_T, \quad q_B^* = 0, \quad a_i^* = \frac{C_A}{N x_i}$$

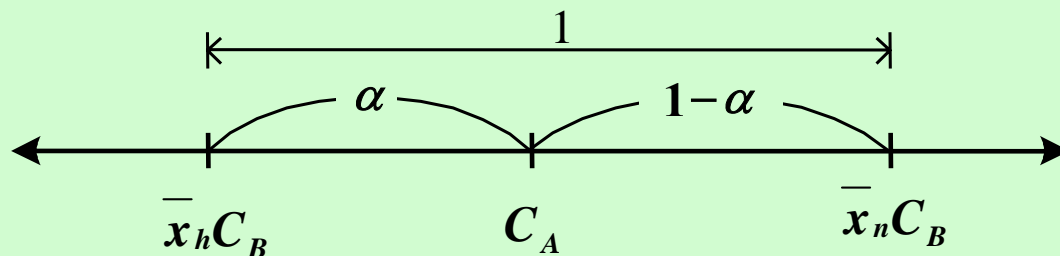
# Steady State Solutions

❖ If  $\bar{x}_h C_B^* < C_A^* < \bar{x}_n C_B^*$  (both resources are bottlenecked together),

$$q_A^* = (1 - \alpha) q_T, \quad q_B^* = \alpha q_T, \quad a_i^* = (1 - \alpha) \frac{\frac{1}{x_i} C_B}{\sum_{i \in N} \frac{1}{x_i}} + \alpha \frac{C_B}{N}$$

where, 
$$\alpha = \frac{C_A - \bar{x}_h C_B}{\bar{x}_n C_B - \bar{x}_h C_B}$$

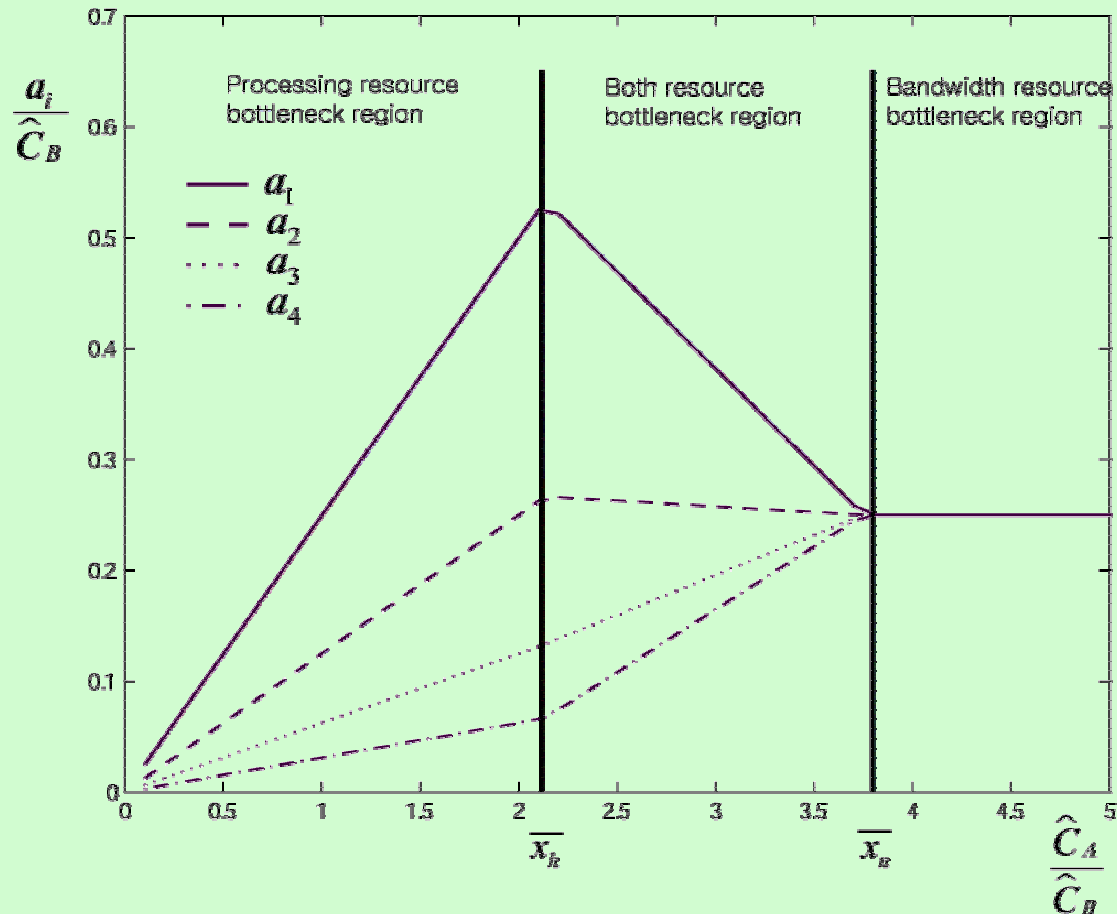
*$\alpha$*  determines the degree of bottleneck intensity.



# Example

4 flows with different  $x_i$  s.

$$(x_1, x_2, x_3, x_4) = (1, 2, 4, 8) \quad \bar{x}_h = 2.13, \quad \bar{x}_n = 3.75$$





# Asymptotic Stability

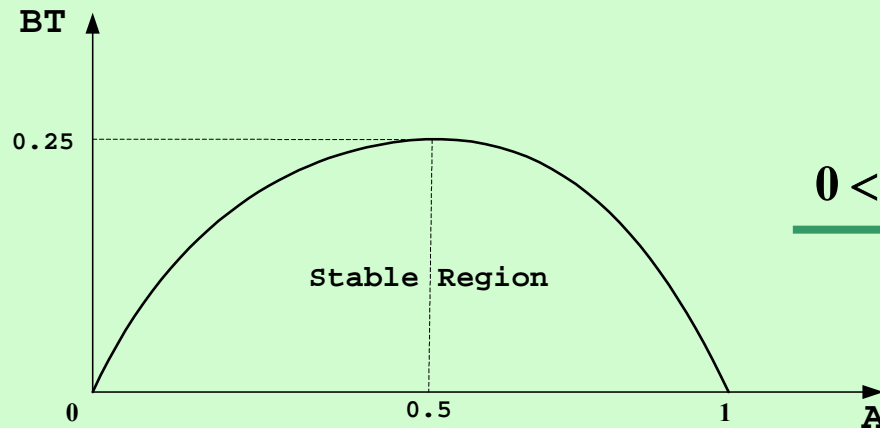
❑ Error function :  $e[k] = q[k] - q_T$

❑ Closed-loop difference equation of  $e[k]$ :

$$e[k+1] - 2e[k] + (1 + A + BT)e[k-1] - Ae[k-2] = 0$$

❑ Characteristic equation :  $z^3 - 2z^2 + (1 + A + BT)z - A = 0$

❑ By **Schür-Cohn Stability Criteria** [7], the closed-loop equation is asymptotically stable if and only if



$$\underline{0 < A < 1, \quad 0 < BT < A(1 - A)}$$

# Asymptotic Decay Rate

## □ Optimal gains

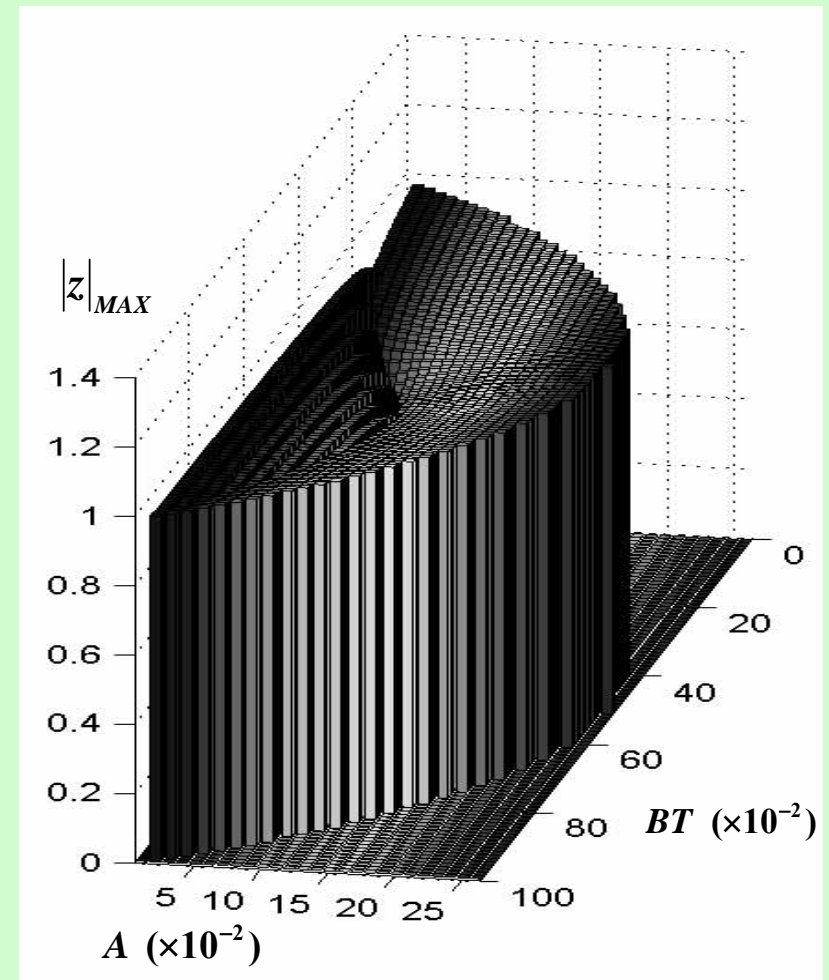
❖ Using numerical analysis,

$$A = 0.32$$

$$BT = 0.05$$

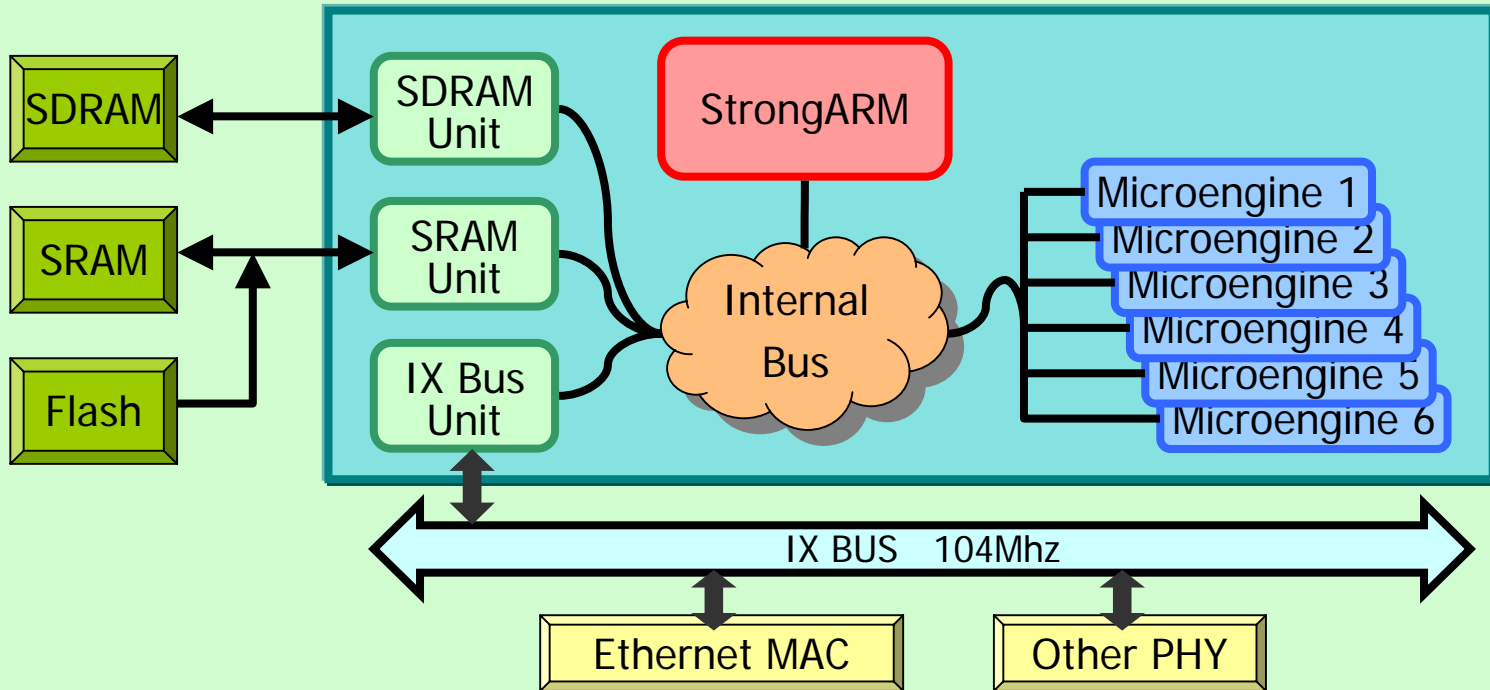
❖ Asymptotic decay rate :

$$0.704 / T$$



# Simulation Environment

## ❑ Intel IXP1200 Evaluation Platform [9]

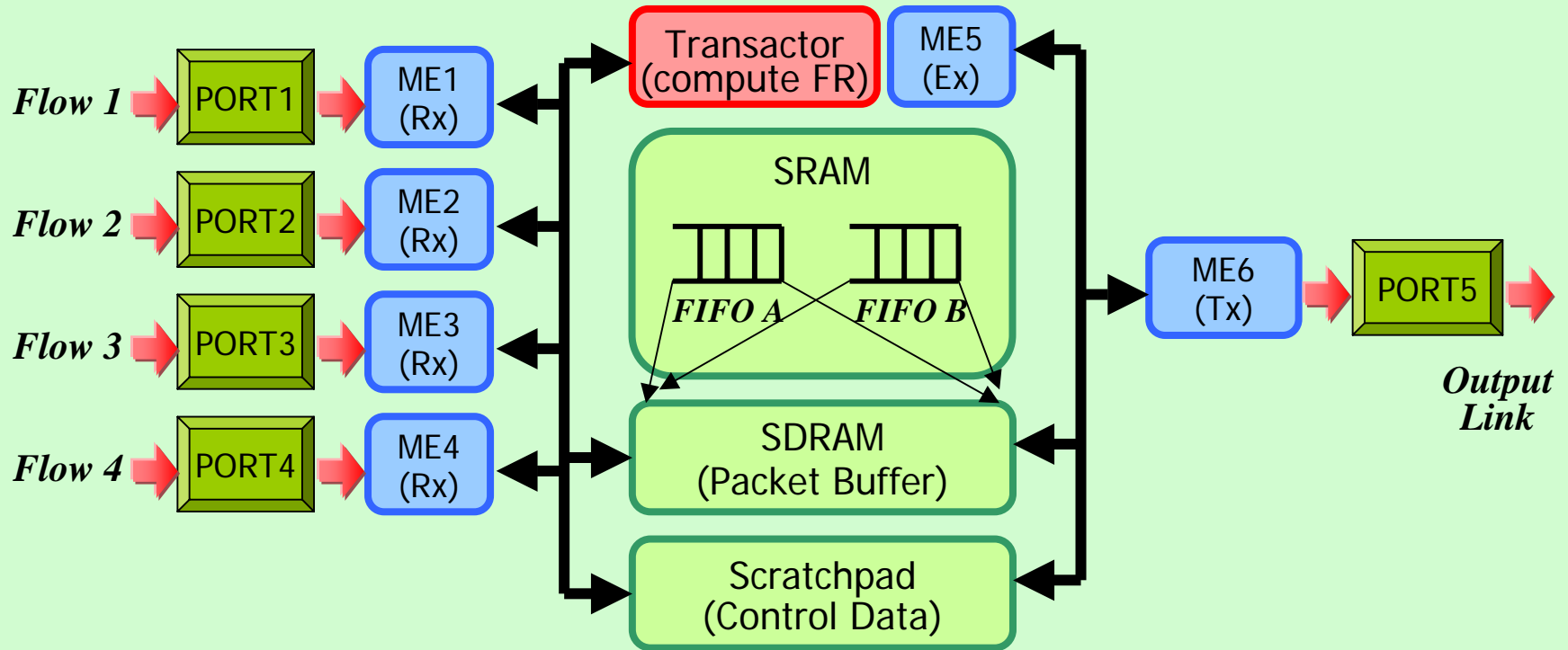


### ❖ IXP1200 Network Processor

- Consists of one StrongARM Core(166Mhz) and six Microengines(166Mhz).
- Provides four hardware contexts with zero context switching overhead in each six microengine.

# Simulation Environment

- Implemented IPv4 (RFC 1812) forwarding engine on ME5.



# Simulation Results

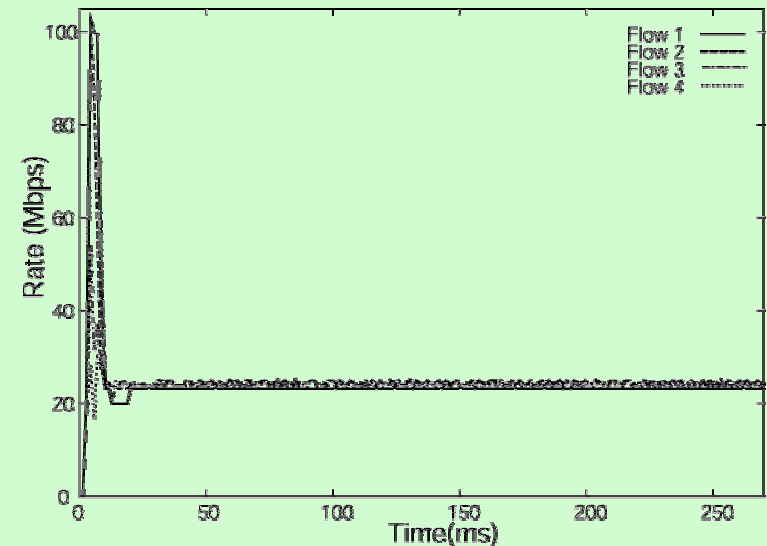
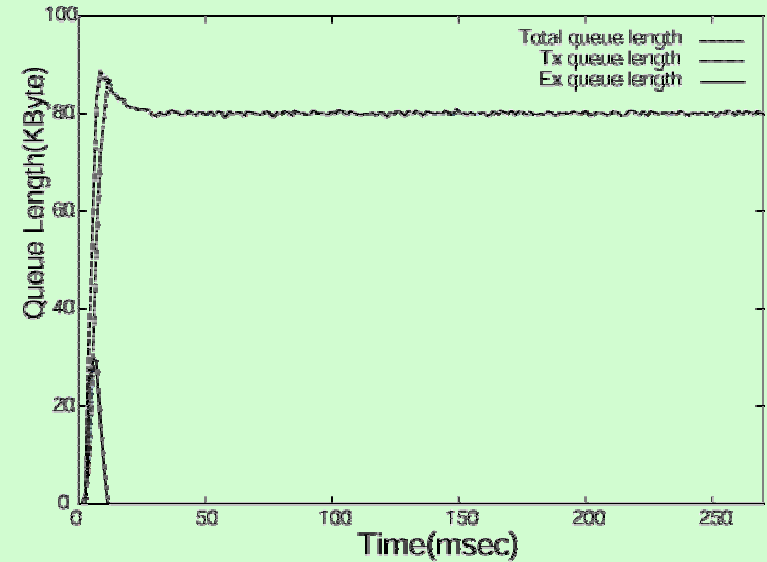
## Bandwidth Resource Bottleneck Case

Flow No.	$x_i$	Fair Rate (Mbps)	Actual Rate (Mbps)
0	2.5	25.0	23.2
1	5.0	25.0	23.8
2	10.0	25.0	24.4
3	20.0	25.0	24.7

$C_B = 100$  Mbps

Tx queue length : 80015 bytes

Ex queue length : 0 bytes



# Simulation Results

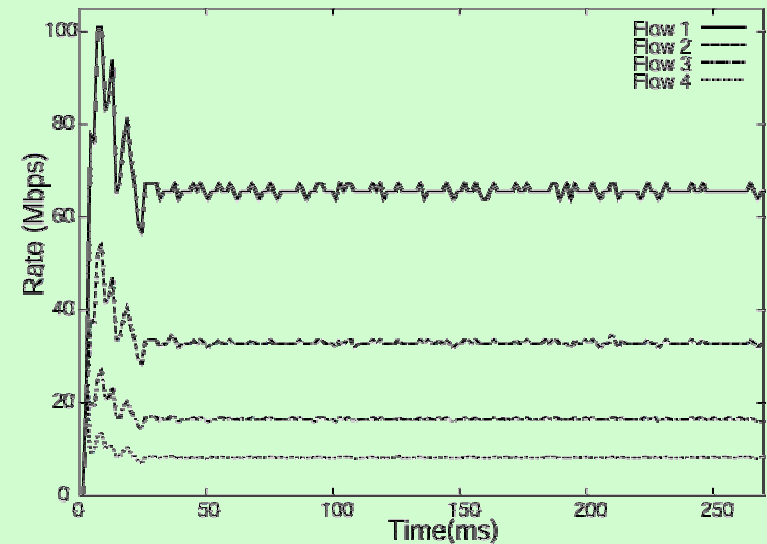
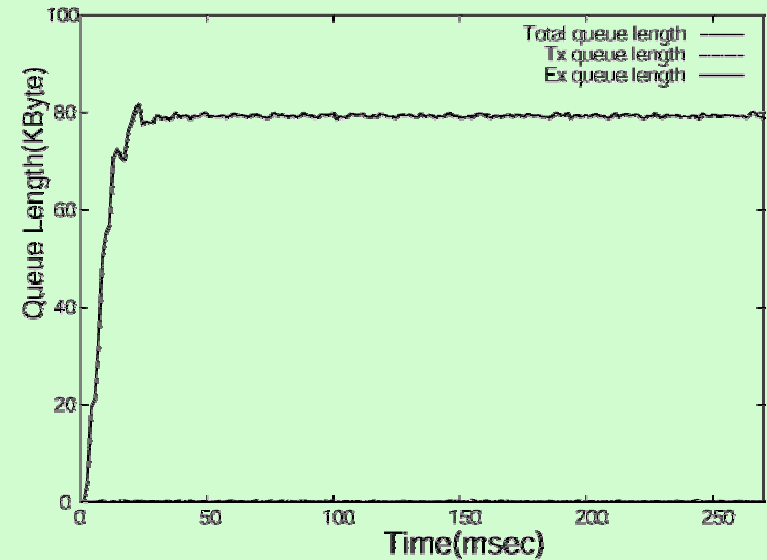
## Processing Resource Bottleneck Case

Flow No.	$x_i$	Fair Rate (Mbps)	Actual Rate (Mbps)
0	4.7	70.8	65.7
1	9.4	35.4	32.9
2	18.8	17.7	16.5
3	37.5	8.9	8.3

$C_B = 300$  Mbps

Tx queue length : 150 bytes

Ex queue length : 79217 bytes



# Simulation Results

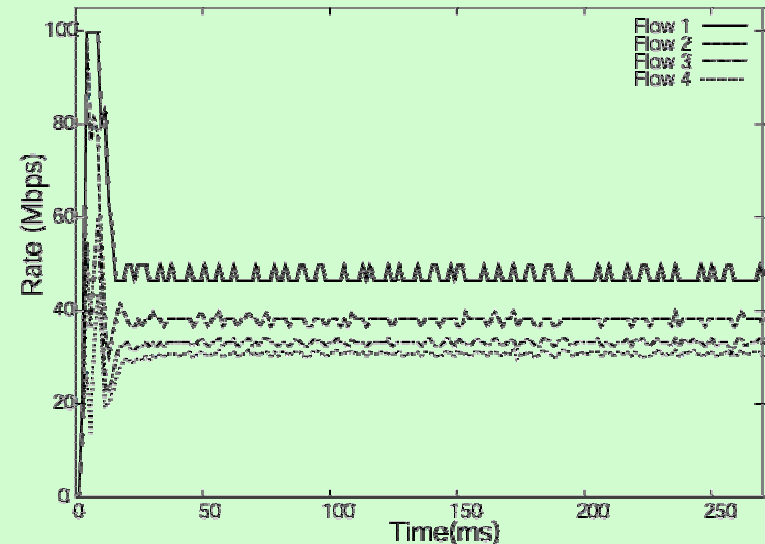
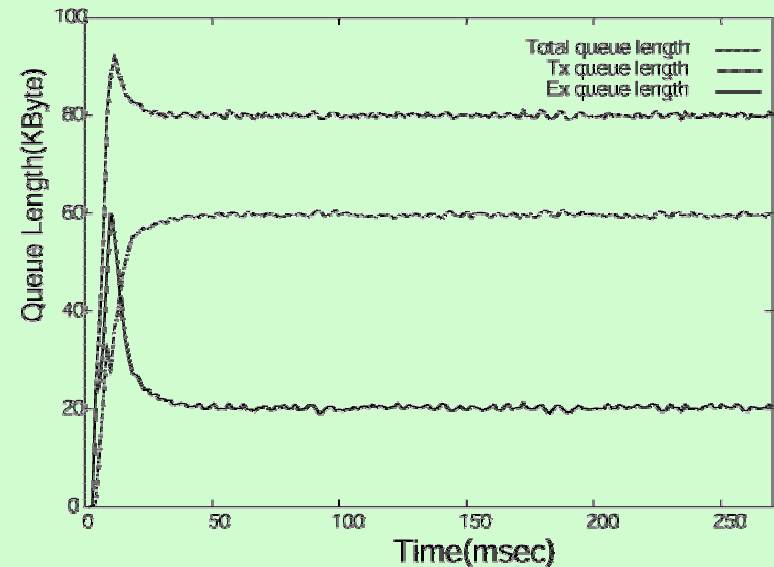
Both Resources Bottleneck Case I  
(BW is more bottlenecked:  $\alpha = 0.746$ )

Flow No.	$x_i$	Fair Rate (Mbps)	Actual Rate (Mbps)
0	2.5	50.3	47.4
1	5.0	40.1	37.9
2	10.0	35.1	33.2
3	20.0	32.5	30.8

$C_B = 158$  Mbps

Tx queue length : 56699 bytes

Ex queue length : 20316 bytes



# Simulation Results

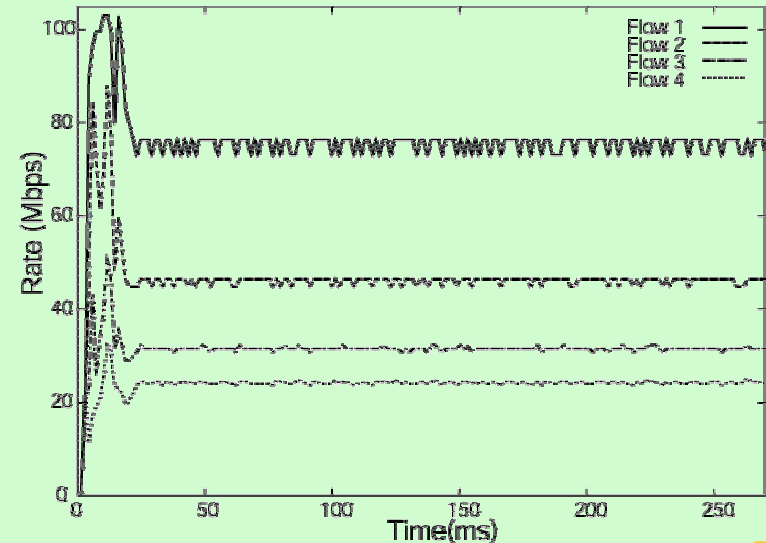
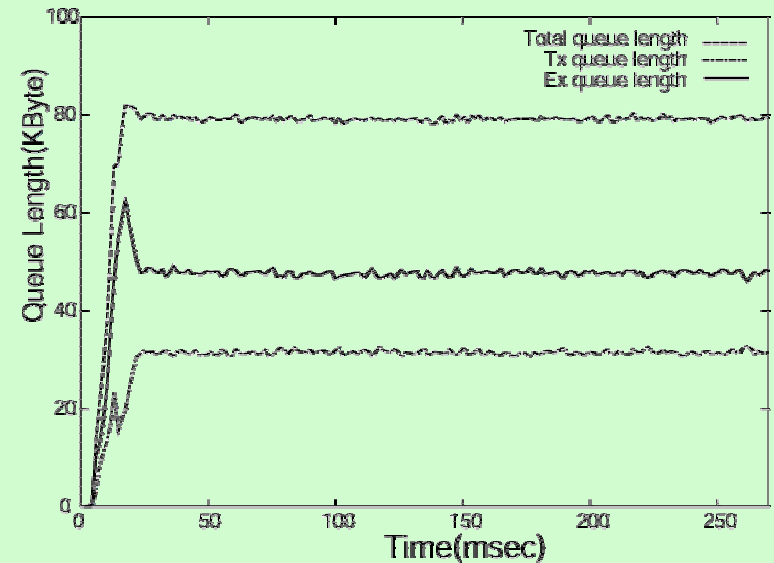
Both Resource Bottleneck Case II  
(CPU is more bottlenecked:  $\alpha = 0.393$ )

Flow No.	$x_i$	Fair Rate (Mbps)	Actual Rate (Mbps)
0	2.5	78.4	75.3
1	5.0	49.1	46.1
2	10.0	34.4	31.5
3	20.0	27.1	24.3

$C_B = 189$  Mbps

Tx queue length : 31441 bytes

Ex queue length : 47703 bytes





# Conclusion

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- ❑ Fair resource allocation when processing time is non-negligible
- ❑ New fairness characterization
- ❑ Control-theoretic algorithm
- ❑ Implementation of IP data path on IXP1200
  
- ❑ Future work
  - ❖ Distributed algorithm for a network of programmable nodes
  - ❖ Understanding in optimization perspective
  - ❖ Microscopic modeling of network processor architecture
  - ❖ Joint management of bandwidth, processing and power

# References

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